Building a dictionary for genomes: Identification of presumptive regulatory sites by statistical analysis

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The availability of complete genome sequences and mRNA expression data for all genes creates new opportunities and challenges for identifying DNA sequence motifs that control gene expression. An algorithm, “MobyDick,” is presented that decomposes a set of DNA sequences into the most probable dictionary of motifs or words. This method is applicable to any set of DNA sequences: for example, all upstream regions in a genome or all genes expressed under certain conditions. Identification of words is based on a probabilistic segmentation model in which the significance of longer words is deduced from the frequency of shorter ones of various lengths, eliminating the need for a separate set of reference data to define probabilities. We have built a dictionary with 1,200 words for the 6,000 upstream regulatory regions in the yeast genome; the 500 most significant words (some with as few as 10 copies in all of the upstream regions) match 114 of 443 experimentally determined sites (a significance level of 18 standard deviations). When analyzing all of the genes up-regulated during sporulation as a group, we find many motifs in addition to the few previously identified by analyzing the subclusters individually to the expression subclusters. Applying MobyDick to the genes derepressed when the general repressor Tup1 is deleted, we find known as well as putative binding sites for its regulatory partners.

The availability of complete genome sequences has facilitated whole-genome expression analysis and led to rapid accumulation of gene expression data from high-density DNA microarray experiments. Correlating the information coded in the genome sequences to these expression data are crucial to understanding how transcription is regulated on a genomic scale.

A great challenge is to decipher the information coded in the regulatory regions of genes that control transcription. So far the development of computational tools for identifying regulatory elements has lagged behind those for sequence comparison and gene discovery. One approach has been to delineate, as sharply as possible, a group of 10–100 coregulated genes (1–3) and then find a pattern common to most of the upstream regions. The analysis tools used range from general multiple-alignment algorithms yielding a weight matrix (4–6) to comparison of the frequency counts of substrings with some reference set (1). These approaches typically reveal a few responsive elements per group of genes in the specific experiment analyzed.

Although multiple copies of a single sequence motif may confer expression of a reporter gene with a minimal core promoter, real genomes are not designed as disjoint groups of genes each controlled by a single factor. Instead, to tailor a gene’s expression to many different conditions, multiple control elements are required and signals are integrated (7). It is assumed that genomewide control is achieved by a combinatorial use of multiple sequence elements. For instance, the microarray experiments for yeast have shown quantitatively that most occurrences of proven binding motifs are in nonresponsive genes, and many responding genes do not have the motif (8, 9). Thus there are multiple sequence motifs to be found (10). Other variables such as copy number and motif position relative to translation start cannot single out the active genes. Regulation by long-range changes in chromosome structure cannot explain the observations in several experiments (8, 9), where 500–1,000 genes that respond are uniformly distributed over the 16 chromosomes. Chromatin structure within the regulatory region can influence transcription, but for the few cases analyzed in detail, this structure is itself under the control of cis-acting elements and therefore amenable to the type of analysis we propose (compare ref. 10). The multiple sequence motifs can be missed because of insufficient sequence data if genes are divided into small subgroups and analyzed separately (11). To detect multiple regulatory elements with optimal statistics, all of the regulatory regions in the genome need to be analyzed together. Alternatively, to identify regulatory elements responsive to a specific genetic or environmental change, all genes that respond in a DNA microarray experiment should be analyzed as a group.

We present an algorithm, “MobyDick,” suitable for discovering multiple motifs from a large collection of sequences, e.g., all of the upstream regions of the yeast genome or all of the genes up-regulated during sporulation. The approach we took formalizes how one would proceed to decipher a “text” consisting of a long string of letters written in an unknown language in which words are not delineated. The algorithm is based on a statistical mechanics model that segments the string probabilistically into “words” and concurrently builds a “dictionary” of these words.

MobyDick can simultaneously find hundreds of different motifs, each of them present in only a small subset of the sequences, e.g., 10–100 copies within the 6,000 upstream regions in the yeast genome. The algorithm does not need external reference data set to calibrate probabilities and finds the optimal lengths of motifs automatically. We illustrate and validate the approach by segmenting a scrambled English novel, by extracting regulatory motifs from the entire yeast genome, and by analyzing data generated from a few DNA microarray experiments.

Theory and Methods

The regulatory sequences in a eukaryotic genome typically have elements or motifs that are shared by sets of functionally related genes. These motifs are separated by random spacers that have diverged sufficiently to be modeled as a random background. The sequence data are modeled as the concatenation of words drawn at random with frequency $p_w$ from a probabilistic “dictionary” $D$; there is no syntax. The words can be of different lengths, and typically regulatory elements emerge as longer words whereas shorter words represent background. Intuitively, to build a dictionary from a text, one starts from the frequency of individual letters, finds over-represented pairs, adds them to the dictionary, determines their probabilities, and continues to

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§1734 solely to indicate this fact.
build larger fragments in this way. The algorithm loops over a fitting step to compute the optimal assignment of \( p_w \) given the entries \( w \) in the dictionary, followed by a prediction step, which adds new words and terminates when no words are found to be over-represented above a certain prescribed threshold.

Given the entries \( w \) of a dictionary (the lexicon), the optimal \( p_w \) is found by maximizing \( Z(S, p_w) \), the probability of obtaining the sequence \( S \) for a given set of normalized dictionary probabilities \( p_w \). For our model,

\[
Z = \sum_p \prod_w (p_w)^{N_w(p)},
\]

where the sum is over all possible segmentations \( P \) of \( S \), i.e., all possible ways in which the sequence \( S \) can be generated by concatenation of words in the dictionary, and \( N_w(P) \) denotes the number of times word \( w \) is used in a given segmentation. For example, if the dictionary \( D = \{A,T,AT\} \) and the sequence \( S = TATA \), then there are only two possible ways \( S \) can be segmented, \( T.A.T.A \) and \( T.A.T.A \). where \( "^2" \) denotes a word separator. The corresponding \( Z(TATA) = (p_A^2 p_T^2 + p_A p_T p_D p_T) \).

For a given set of dictionary words \( w \), we fit the \( p_w \) to the sequence \( S \) by maximizing the likelihood function in Eq. 1 with the constraint that \( p_w \geq 0 \) and \( \sum_w p_w = 1 \). This condition is equivalent to solving for \( p_w \) from the equation

\[
p_w = (N_w)/\sum_w (N_w),
\]

where \( (N_w) = p_w (\partial / \partial p_w) \ln Z \) is the average number of words \( w \) in the ensemble defined by \( Z \). The right hand side of Eq. 2 can, of course, be defined for an arbitrary dictionary, and it is very fruitful to interpret Eq. 2 as a map or discrete dynamical system, i.e., an arbitrary set of \( p_w \) is inserted on the right and generates a new set, \( p_w \), on the left. The fixed point of this map is equivalent to the extremal condition on Eq. 1. Eq. 2 can be solved by simple iteration, and at each step \( Z \) increases. This can be quite slow because when the right-hand side of Eq. 2 is linearized around the current value of \( p_w \) by taking a derivative, the resulting matrix has eigenvalues close to 1. However, given this matrix we can raise it to the power of \( 2^n \) by doing \( n \) matrix multiplications. These product matrices can be used to approximate the result of \( 2^n \) iterations of Eq. 2, and we take the largest \( n \) such that \( Z \) increases and \( p_w \) stay positive. When the \( p_w \) are close enough to the fixed point so that all of the eigenvalues are less than 1 (the map contracts) we switch to Newton’s method to find the fix point to machine accuracy.

A dynamic programming-like technique, similar in spirit to transfer matrix methods in statistical mechanics, permits the computation of \( Z \) and its various derivatives (up to the second order) in \( O(LD^2) \) operations where \( L \) is the total sequence length, \( D \) the dictionary size, and \( L \) the maximum word length. (Further details are available elsewhere3.) Computation of the averages on the right-hand side of Eq. 2 by Monte Carlo methods would be hopelessly inaccurate for our purposes. If the defining words are known, the statistical errors on \( p_w \) are set by the Gaussian fluctuations of the background, e.g., if \( p_A_{A,G,T} \) is 1/4 and there is only one other word in the text in length \( \ell \), its probability is uncertain by \( (L^4)^{-1/2} \). Our algorithm handles dictionaries up to \( 10^6 \) words routinely, and we have verified that the maximum is unique by randomizing the starting \( p_w \) and reconverging.

In the prediction step, we do statistical tests on longer words based on their predicted frequencies from the current dictionary. For example, if the current dictionary \( D \) is \( \{A,T,AT\} \), then the expected frequency of the length-3 word \( TAT \) (assumed to be embedded in a longer string) can be deduced from the various ways it can be made by concatenations of the words in the dictionary: \( ATAT, ATAT, TATAT, \) and \( TATAT \). Note that the occurrence of a word is contingent on a partition; its frequency is the total probability of all partitions that delimit it, which has no simple relation to the number of times the substring occurs in the data. In practice, to check the completeness of the dictionary, we consider all pairs of dictionary words \( w,w' \) and ask whether the average number of occurrences of the composite word \( w,w' \) created by juxtaposition exceeds by a statistically significant amount the number predicted by the model3, (\( N_w(N_{w'}) \)). If so, the composite word is added to the dictionary. Here the statistical significance of longer words is based on the probability of shorter words, thus eliminating the need for an external reference data set to define probability. It should be noted that the background model for the statistical test evolves as the dictionary grows. Most other models assume a static background (1, 4–6, 12).

Although the juxtaposition of dictionary words is a very efficient means for narrowing the search for underpredicted strings, it can miss words that are not built from fragments already in the dictionary. Thus we have designed routines to search for over-represented motifs exhaustively within certain classes. In addition to specific strings, we search for clusters of strings defined by including up to two International Union of Pure and Applied Chemistry symbols representing the 12 distinct subsets of two or more bases. Even if the frequency distribution of all strings up to a given length is consistent with Gaussian fluctuations, there can be correlations among the fluctuations and thus meaningful signals in the cluster. Motivated by many biological examples, we also searched for motifs consisting of two short strings separated by a gap, so-called dimers. Once new motifs are added to the dictionary, the new maximization step tests the relevance of all words in parallel and sets to zero the probabilities of less specific words when a more specific one will account for the over-represented string. Once a piece of a motif has been found, it can be grown or contracted (by adding or removing letters) again in parallel for all motifs. In this way words with optimal lengths will emerge.

Having the dictionary still does not permit one to “read” the text in a unique way, because the decomposition into words is probabilistic, and there are many ways to segment the data into words; yet key words do emerge. Let \( \Xi_w \) be the number of matches to the word \( w \) anywhere in the sequence, and \( (N_w) \) the average number of times the string \( w \) is delimited as a word among all segmentations of the data; then the ratio \( (N_w)/\Xi_w \) serves as a quality factor. When the ratio is close to one, almost all occurrences of the string \( w \) are attributed to the word \( w \) itself, instead of being made by concatenations of other words; thus the word \( w \) can be clearly delineated from the background. The dictionary does not distinguish between signal and background, although shorter words typically have lower quality. Methods based on frequency counts \( \Xi \) will register as significant (i.e., over-represented) any substring overlapping with a dictionary

\[\text{To convert the observed number of words} \ w \ \text{created by juxtaposition, from underrepre-}\]

sented \( n \)-mer counts in the sequence, \( \Xi_w \) clustering of \( n \)-mers, etc., into a probability we subtract the mean and divide by the standard deviation (both as predicted by the current dictionary) to get a \( z \)-score, \( \sigma_w \). The threshold value for adding a word \( w \) when is given by \( \sigma_w < 1/N_w \) where \( (N_w) \) is the probability of having a \( z \)-score larger than \( \sigma_w \) based on a unit Gaussian, and \( N_w \) is the total number of words in the category being examined. For juxtaposition the expected mean and deviation are computed from the probabilities of the various segmentations as was done for Eq. 2 and its derivative. For the \( n \)-mer counts, we simply prepared a large number of synthetic copies of the sequence data by drawing from the dictionary and counted the number of copies of each string. For \( 1 \)-2 Mb of data, \( n < 8 \) is the limit imposed by statistics. Similarly for dimers we took examined all pairs of \( n \)-mers (of length \( n < 5 \)) separated by a gap of 3–10 N symbols (matching any base).
word, whereas our fit will assign $p_w > 0$ only to the dictionary word itself.

**Results**

It is instructive to validate the performance of our algorithm with English text. We took a portion of the novel *Moby Dick* comprising $\approx 10^5$ characters (the first 10 chapters) and reduced it to a lowercase string containing no spaces or other punctuation characters. The starting dictionary was just the English alphabet; words were added by juxtaposition only and were required to have at least two copies in the data. The original text had 4,214 unique words of which 2,630 were a single copy, which our algorithm was forced to break up. The final dictionary had 3,600 words. Among the most significant 1,800 were 800 English words, 800 were concatenations of English words, and only 200 were fragments. Virtually all of the 1,600 text words with two or more copies occurred somewhere in our dictionary. To mimic the biological situation, we also introduced random letters (whose frequency matched the text) between each word to increase $L$ by a factor of 3. The final dictionary then had 2,450 words. Among the most significant 1,050 were 700 English words and 40 composite words.

In a sense English is too simple: as the probability of obtaining longer words by chance is very small, simply checking for all strings with two or more copies would identify many words. Biological data are different: virtually all 8-mers have two or more copies in the combined upstream regions in yeast, yet less than 1% occur in our dictionary as described below.

A dictionary was prepared for all of the upstream regions in the yeast genome. To maximize the homogeneity of our data, we define control regions to extend upstream from the translation start site to the next coding region on either strand but not more than 600 bp. All exact repeats longer than 6 bases were removed. This operation removed 14% of the data. Starting from a single-base dictionary, words were added via an exhaustive search procedure. We experimented with many ways of adding words to the dictionaries. For the data presented here, we added over-represented $n$-mers for lengths increasing from $n = 1$ to $n = 8$; subsequently, words in the dictionary were allowed to grow one base at a time if the extended word was over-represented. All significant motifs with at most two Inter- national Union of Pure and Applied Chemistry symbols, and a total of eight characters then were added. We imposed a minimum of two copies for any dictionary entry.

The final dictionary had 1,200 words, of which 100 were clusters of similar oligonucleotides. On average, two-thirds of the sequence data were segmented into single-letter words and an additional 15% into words of length 4 or less. About 500 dictionary entries fell above a plausible significance level as defined by the quality factor. These included good matches to about half of the motifs found in refs. 1, 8, and 9, including the MCB, SCB, and MCM1 cell-cycle motifs and the URS1 motif for sporulation (Table 1). We also found $\approx 400$ words in the form of two short segments separated by a gap, the most significant of which clustered together to generate the motifs in Table 2.

Table 3 gives a more comprehensive measure of the extent to which our dictionary is predicting functional biological sites by comparing it with a database of experimentally determined sites (13). This database of experimentally confirmed regulatory sites in yeast has entries covering $\approx 200$ genes and $\approx 110$ factors. Almost all sites occur upstream of the translation start. For comparison with this database, we filtered our dictionaries based on a significance score $[N_w / \bar{E}_w > 0.2$ and $\bar{E}_w \leq 100$, to filter out poly(A) and similar strings] and matched (by inclusion) against the 443 nonrepetitive sites of length 5–30. The number of sites hit by chance is calculated by marking the dictionary words on the sequence data (to account for correlations) and then treating the database entries as intervals to be placed at random. Of the 443 nonredundant sites in the database, we hit 114 with a combination of compact words (words with no gaps in the middle) and dimers (two short segments separated by a variable gap), which is 18 standard deviations beyond expectation. As an additional control for the statistical significance of our matches, we scrambled the dictionary words by randomly permuting the letters in each word, and then matched them against the data.

Table 2. A sample of the motifs assembled by clustering the most statistically significant word pairs of length 4–5 with a spacing of 3–30 from a genomewide dictionary

<table>
<thead>
<tr>
<th>Motif</th>
<th>Factor (13)</th>
<th>$-\log_{10}(P)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>KHCGHTHNNNTNGAYW</td>
<td>ABF1</td>
<td>28</td>
</tr>
<tr>
<td>ATRCACTNNNNACGCD</td>
<td>RAP1, ABF1</td>
<td>52</td>
</tr>
<tr>
<td>TTTCCNNNNNGGAAA</td>
<td>MCM1</td>
<td>4</td>
</tr>
<tr>
<td>ATACANNNNNTACAT</td>
<td>?</td>
<td>10</td>
</tr>
<tr>
<td>CGGTNNTNNGGGAT</td>
<td>?</td>
<td>9</td>
</tr>
<tr>
<td>GGGCNNNNNNACCGG</td>
<td>?</td>
<td>7</td>
</tr>
<tr>
<td>CACGTGNNNNNNCAGTG</td>
<td>?</td>
<td>7</td>
</tr>
</tbody>
</table>

The clusters were sharp enough that all the word pairs in a cluster aligned. The probability cutoff is $-\log_{10}$ of the total number of the pairs sampled, $(533)^2 \approx 28$ for the homodimers and $30 \times 533$ for the homodimers, where 533 is the total number of words of length 4–5. The probability score for the most significant dimer in the cluster is tabulated.
base. In contrast to less systematic assignments of probability, our dictionary correctly predicts the copy number of all strings of length 8 or less, plus certain classes of clusters of which the members are related by a couple of single-base mutations. Thus we can say that for the categories of motifs that we searched for exhaustively, ≈74% of the experimental sites are not statistically over-represented. This statistic, of course, does not exclude the possibility that some of these experimental sites escape our detection because of their great variability or that some of the experimental assignments are incorrect. It is difficult to assess our false-positive rate, because the database covers such a small fraction of the genome.

The above whole-genome analysis uses only information from the genome sequence and is independent of context. For cases in which the responses of all of the genes to a specific genetic or environmental perturbation are measured, a context-dependent dictionary can be constructed by applying MobyDick to a subset of genes that are active under a particular condition, and words in the dictionary can be more readily correlated with the existing knowledge base. We illustrate this approach by analyzing two DNA microarray experiments carried out on yeast: sporulation and TUP1 deletion.

A dictionary was built for the ≈500 genes that are up-regulated during sporulation (9). Using the most stringent criterion for word addition, the sporulation dictionary had only 250 unique words, of which 150 were significant; 66% of the data were segmented into single-letter words and an additional 22% of length 4 or less. The two known principal sporulation elements, URS1 and MSE, have consensus motifs 5′-DSGGCGGC and 5′-CRCAAAW (9). Dictionary words that strongly overlap with these patterns are TCGGCGGC, GGCGGCAAA, TGGGCG-CRAAAW (9). Dictionary words that strongly overlap with and DNA microarray experiments carried out on yeast: sporulation knowledge base. We illustrate this approach by analyzing two in the dictionary can be more readily correlated with the existing dictionary can be constructed by applying MobyDick to a subset of the genome sequence and is independent of context. For cases our false-positive rate, because the database covers such a small fraction of the genome.

### Table 3. Statistics of matches to the yeast promoter database of ref. 13

<table>
<thead>
<tr>
<th>Data set</th>
<th>Observed</th>
<th>Expected ± SD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Compact words</td>
<td>94</td>
<td>23 ± 4.8</td>
</tr>
<tr>
<td>Dimers</td>
<td>26</td>
<td>2.7 ± 1.8</td>
</tr>
<tr>
<td>Scrambled dictionary</td>
<td>33</td>
<td>14 ± 3.3</td>
</tr>
<tr>
<td>Ref. 12</td>
<td>30</td>
<td>9 ± 2.9</td>
</tr>
</tbody>
</table>

Table 3 shows the statistics of matches to the yeast promoter database of ref. 13. The first two entries list the matches by the compact words (words with no gap) and dimers (two short segments separated by a variable gap) in our dictionary. The third entry gives the statistics after the words are scrambled by a random permutation of the letters in each word. For the last entry, we cut off the list of motifs from ref. 12 ordered by significance when the total number of Ξ counts in the data equaled that for the dictionary set (approx. 21,000). All other filters were identical.

The first two entries list the matches by the compact words (words with no gap) and dimers (two short segments separated by a variable gap) in our dictionary. The third entry gives the statistics after the words are scrambled by a random permutation of the letters in each word. For the last entry, we cut off the list of motifs from ref. 12 ordered by significance when the total number of Ξ counts in the data equaled that for the dictionary set (approx. 21,000). All other filters were identical.

### Table 4. Several of the most significant word clusters from our sporulation dictionary that also are over-represented in one or more of the subgroups of the sporulation genes

<table>
<thead>
<tr>
<th>Motif</th>
<th>Observed</th>
<th>Expected</th>
<th>Classes</th>
</tr>
</thead>
<tbody>
<tr>
<td>TCAGGTCA/CTGTGCA/CTGTGTC</td>
<td>35</td>
<td>7</td>
<td>4</td>
</tr>
<tr>
<td>TGGCCAGC/GGCCCA/CGGCCCT</td>
<td>52</td>
<td>2</td>
<td>4</td>
</tr>
<tr>
<td>GCGCGCAG/GCCCG/GAGGCGG/GAGGCGA/GAGGCGAC/GCGGCGG</td>
<td>18</td>
<td>3</td>
<td>1, 2, 5</td>
</tr>
<tr>
<td>GCGCGGTA/CGGCGCCA/CGGCGCTAAA</td>
<td>10</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>CGTCACAAA/GTCACAAAA</td>
<td>17</td>
<td>1</td>
<td>4</td>
</tr>
</tbody>
</table>

Table 4 lists several of the most significant word clusters from our sporulation dictionary that also are over-represented in one or more of the subgroups of the sporulation genes. The statistics include the number of copies of the motif in the corresponding temporal classes (column 2), and number expected based on the total counts in all promoters (column 3). The last two entries are elaborations of the URS1 and MSE motifs that better discriminate responding from nonresponding genes.
sufficient to derepress certain classes of genes and that certain activators also are required. We also missed the binding site for another Tup1 partner, Cr1, which represses DNA-damage-inducible genes, of which several examples are in the data set. The frequency of the Cr1 site is fit well by our dictionary and thus is not over-represented.

Discussion

We have implemented an algorithm that does a maximum-likelihood fit of data sets as large as several megabases to a probabilistic model: words drawn at random from a dictionary with prescribed frequency. The algorithm loops over a frequency estimation step for a known set of words, followed by the generation of new words by comparing the model predictions with the data. The first step quantifies the probabilities attached to each segmentation of the data, the number of which scales exponentially with the data length. The average base in the sequence typically will be part of several words. Although the probability estimation step converges to a unique global optimum, the word addition step is more heuristic. Namely, we only check that the model fits the data for a limited set of patterns, i.e., n-mers (up to length 8), clusters thereof, dimers, and words formed by juxtaposing dictionary entries.

The dictionary words can be ordered by their quality factor, \( \langle N_w \rangle / \Sigma w \), which represents the fraction of occurrences of the string \( w \) in the data that are delineated as words by our model, not the result of a chance juxtaposition of other words or word fragments. It is natural to use the quality factor to distinguish words of potential biological significance from those that parameterize the “background.” Our fit is very sensitive: \( p_w \) will be nonzero if \( \Sigma w \) differs by more than \( \sqrt{N} \) from the value expected for when the word \( w \) is absent. Words at the limit of detection will have a quality factor that scales as \( 1/\sqrt{N} \). Short words invariably have low quality factors, but certain long words such as poly(A) do also, when there is a large size range of such sites in the data.

Our algorithm has extracted with high statistical significance many known cis-regulatory elements from data sets as large as the entire yeast genome, using no other empirical information. By contrast for the much smaller sporulation data set, MEME (6) only found the URS1 and MSE sequences (and a weak third motif) after the data were further divided into seven clusters (9). We found these, plus \( \approx 20 \) others, several of which matched experiments (14, 18, 19) plus a statistically significant portion of motif) after the data were further divided into seven clusters (9). Hidden Markov models (23) are a common way to segment biological data, but they generally are used with relatively few segment types (e.g., promoter, exon, intron) each described by many parameters; we work with many segments, most described by a single parameter.

Our algorithm admits many elaborations such as identifying reverse complements and incorporating an additional degree of freedom into our maximum-likelihood method to segment the data into regions each with a different dictionary. Weight matrices also can be introduced in this way. Even in its present form, our algorithm, if allowed to fit an entire yeast chromosome with all words length 4 or less, will put 99% of the weight into length 3 words (codons) and place almost all of the other length words into noncoding regions.

We cannot yet treat long, fuzzy patterns such as protein motifs over the 20-letter alphabet, for which weight matrix methods were designed (4–6). There are many interesting motifs in yeast, however, which are less than 10 bp long and have only a few variable sites, which we can readily detect.

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